

Shape and Space V (4) Area of non right angled triangles

Do now:

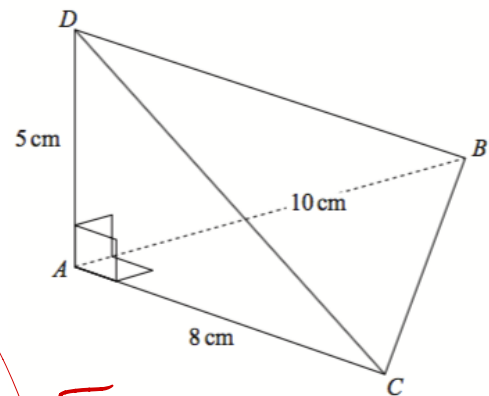
The diagram shows a tetrahedron.

AD is perpendicular to both AB and AC.

Angle BAC = 90°.

Calculate the size of angle BDC.

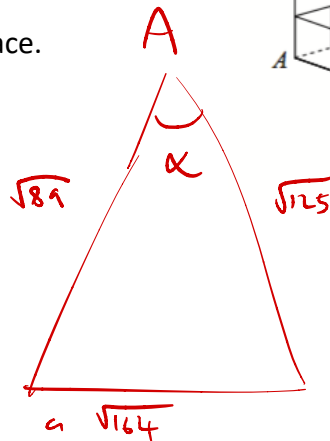
Give your answer correct to 1 decimal place.



$$DC = \sqrt{5^2 + 8^2} = \sqrt{89}$$

$$DB = \sqrt{10^2 + 5^2} = \sqrt{125}$$

$$BC = \sqrt{8^2 + 10^2} = \sqrt{164}$$

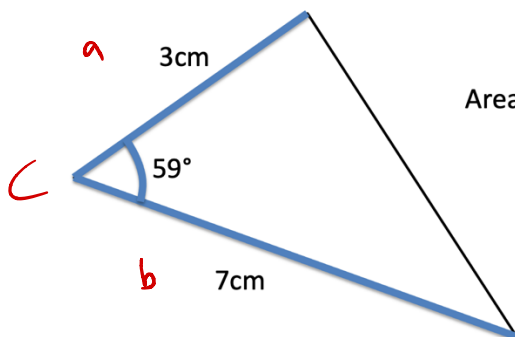


$$A = \cos^{-1} \left[\frac{b^2 + c^2 - a^2}{2bc} \right]$$

$$A = 76.3^\circ$$

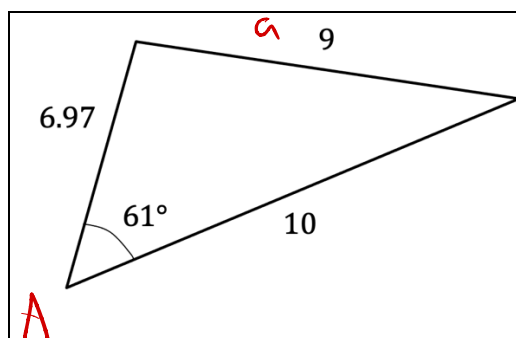
$$\text{Area} = \frac{1}{2} a b \sin(C)$$

Where C is the angle wedged between two sides a and b.



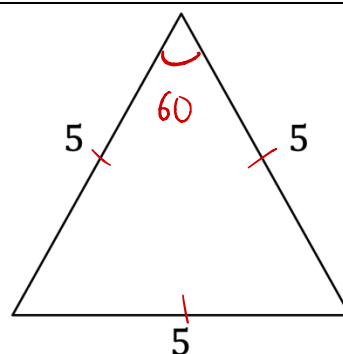
$$\text{Area} = \frac{1}{2} (3)(7) \sin 59 = \underline{\underline{9.00 \text{ cm}^2}}$$

EQUILATERAL



$$\text{Area} = \frac{1}{2} (6.97)(10) \sin 61$$

$$= 30.48$$



$$\text{Area} = \frac{1}{2} (5^2) \sin 60$$

$$= \frac{25\sqrt{3}}{4}$$

Harder examples

$ABCD$ is a parallelogram.

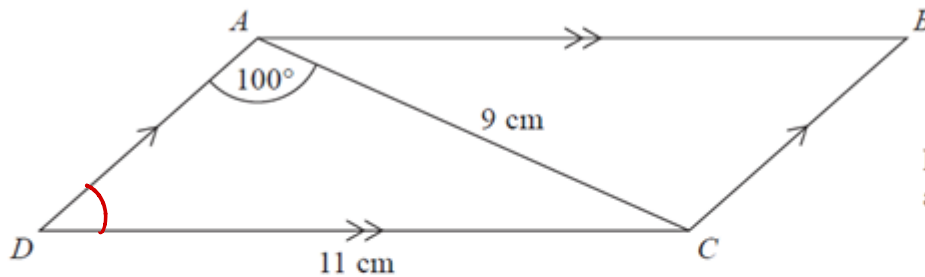


Diagram **NOT** accurately drawn

$AC = 9$ cm

$DC = 11$ cm

Angle $DAC = 100^\circ$

Calculate the area of the parallelogram.

Give your answer correct to 3 significant figures.

CALCULATE $\angle ADC$

$$\frac{\sin D}{a} = \frac{\sin 100}{11}$$

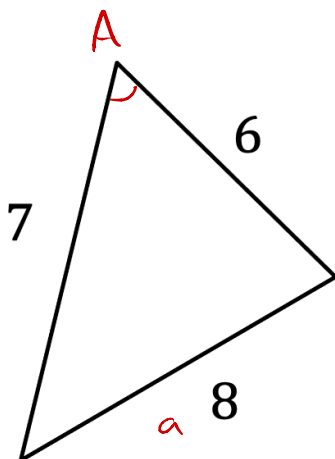
$$D = 53.6829^\circ$$

$$\therefore \angle ACD = 180 - 100 - 53.6829 = 21.945^\circ$$

$$\begin{aligned} \text{AREA}_{ADC} &= \frac{1}{2} (9)(11) \sin(21.945) \\ &= 21.945 \end{aligned}$$

$$\text{AREA}_{ABCD} = 2 \times 21.945 = \underline{\underline{43.9 \text{ (3sf)}}}$$

Q2

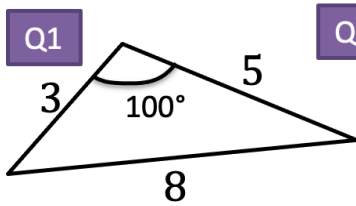


$$A = \cos^{-1} \left[\frac{7^2 + 6^2 - 8^2}{2(7)(6)} \right]$$

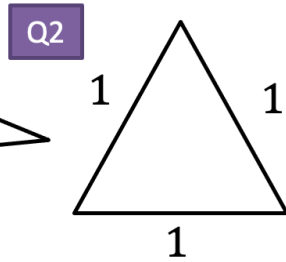
$$A = \underline{\underline{75.5^\circ}}$$

$$\begin{aligned} \text{AREA} &= \frac{1}{2} (7)(6) \sin(75.3) \\ &= \underline{\underline{20.3}} \end{aligned}$$

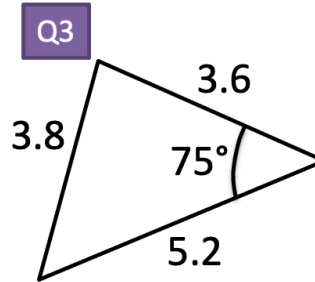
Calculate the areas of the triangles



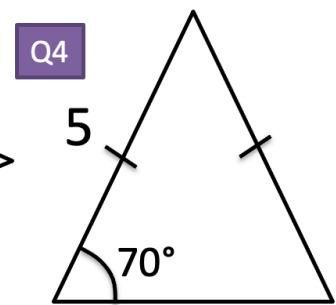
$$A = 7.39$$



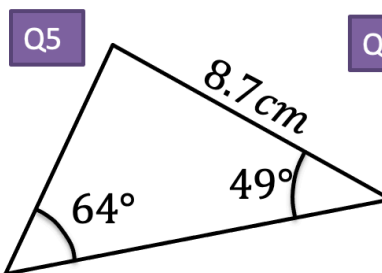
$$A = \frac{\sqrt{3}}{4} = 0.433$$



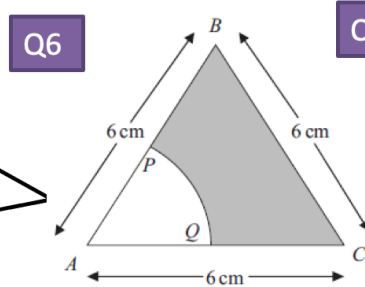
$$A = 9.04$$



$$A = 8.03$$

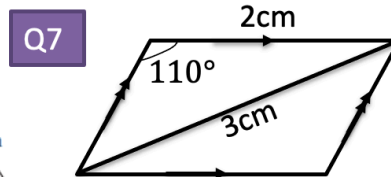


$$A = 29.25 \text{ cm}^2$$

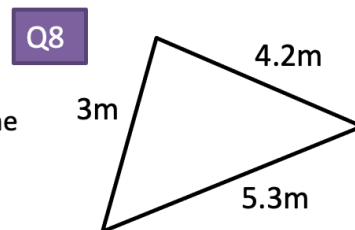


P is the midpoint of AB and Q the midpoint of AC. APQ is a sector of a circle. Find the shaded area.

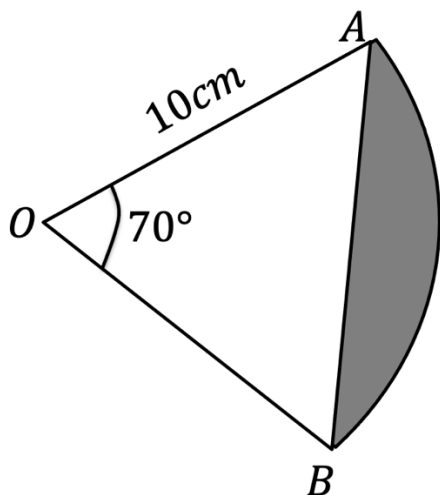
$$A = 10.9 \text{ cm}^2$$



$$A = 3.11 \text{ cm}^2$$

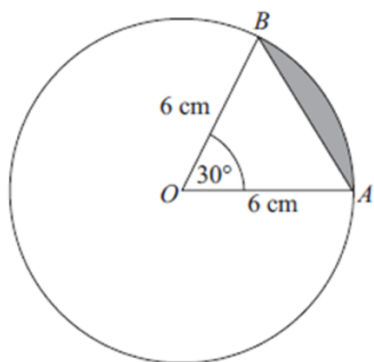


$$A = 6.29 \text{ m}^2$$



OAB is a sector of a circle, centred at O .
Determine the area of the shaded segment.

$$\begin{aligned}\text{Area of sector} &= \frac{70}{360} \pi (10^2) = 61.0865 \text{ cm}^2 \\ \text{Area of triangle} &= \frac{1}{2} (10)^2 \sin 70 = 46.9846 \text{ cm}^2 \\ \text{Area of segment} &= 61.0865 - 46.9846 \\ &= 14.1 \text{ (3sf.)}\end{aligned}$$



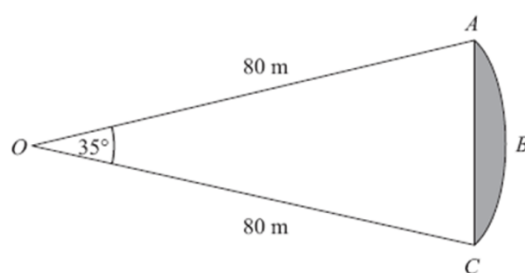
The diagram shows a circle, centre O .
 A and B are points on the circle.
 $OA = OB = 6 \text{ cm}$.

The value of $\sin 30^\circ = \frac{1}{2}$

Work out the area of the shaded segment.
Give your answer in terms of π .

$$A = \frac{30}{360} \pi (6^2) - \frac{1}{2} (6^2) \sin 30$$

$$A = 3\pi - 9$$



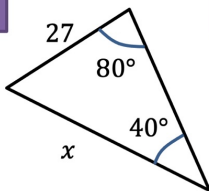
ABC is an arc of a circle centre O with radius 80 m .
 AC is a chord of the circle.
Angle $AOC = 35^\circ$.

Calculate the area of the shaded region.
Give your answer correct to 3 significant figures.

$$A = \frac{35}{360} \pi (80^2) - \frac{1}{2} (80^2) \sin 35$$

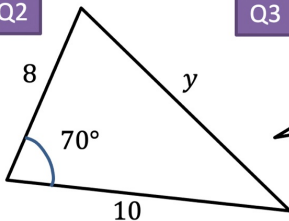
$$A = 119 \text{ m}^2$$

Q1



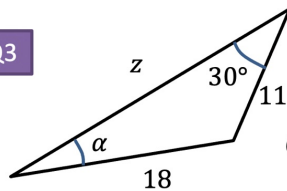
a) $x = 41.37$
b) Area = 483.63

Q2



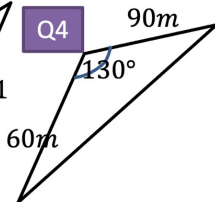
$y = 10.45$
Area = 37.59

Q3



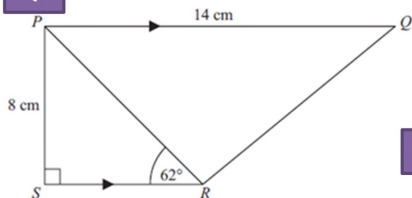
$\alpha = 17.79^\circ$
 $z = 26.67$
Area = 73.33

Q4



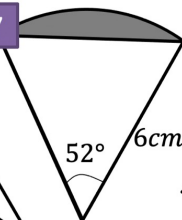
Perimeter = 286.5m

Q5



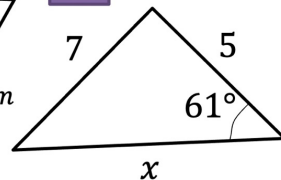
$QR = 12.6$ cm

Q7



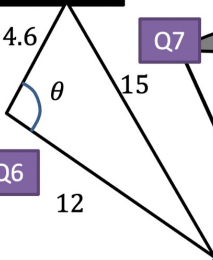
Area = 2.15 cm²

Q8



$x = 7.89$
Area = 17.25

Q6



$\theta = 122.8^\circ$